International Journal of Current Advanced Research

ISSN: O: 2319-6475, ISSN: P: 2319-6505, Impact Factor: 6.614

Available Online at www.journalijcar.org

Volume 7; Issue 4(J); April 2018; Page No. 11961-11964 DOI: http://dx.doi.org/10.24327/ijcar.2018.11964.2089



MULTIPLICATIVE CONNECTIVITY ve-DEGREE INDICES OF DOMINATING OXIDE AND REGULAR TRIANGULATE OXIDE NETWORKS

Kulli V.R*

Department of Mathematics, Gulbarga University, Gulbarga 585106, India

ARTICLE INFO

Article History:

Received 17th January, 2018 Received in revised form 26th February, 2018 Accepted 9th March, 2018 Published online 28th April, 2018

Key words:

Multiplicative connectivity ve-degree indices, dominating oxide network, regular triangulate oxide network.

ABSTRACT

In Chemical Graph Theory, connectivity indices have been found useful in practical application. Recently, the ve-degree concept is defined in Graph Theory. In this paper, we introduce the multiplicative product connectivity ve-degree index, multiplicative sum connectivity ve-degree index, multiplicative atom bond connectivity ve-degree index and multiplicative geometric-arithmetic ve-degree index of a molecular graph. Furthermore we compute these multiplicative connectivity ve-degree indices of chemically interesting networks like dominating oxide and regular triangulate oxide networks.

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INTRODUCTION

A molecular graph is a simple graph related to the structure of a chemical compound. Each vertex of this graph represents an atom of the molecule and its edges to the bond between atoms. A topological index is numerical parameter mathematically derived from the graph structure. Chemical Graph Theory is a branch of Mathematical Chemistry which has an important effect on the development of chemical sciences. There are many topological indices that have some applications in Chemistry, see [1].

Let G be a finite, simple connected graph with vertex set V(G) and edge set E(G). The degree $d_G(v)$ of a vertex v is the number of vertices adjacent to v. Let S_v denote the sum degrees of all vertices adjacent to a vertex v. We call S_v as sum degree. The set of all vertices which adjacent to v is called the open neighborhood of v and denoted by N(v). The set $N(v) \cup \{v\}$ is called the closed neighborhood of v and denoted by N[v].

In [2], Chellali et al. defined the ve-degree concept in Graph Theory as follows:

The ve-degree $d_{ve}(v)$ of a vertex v in a connected graph G is the number of different edges that incident to any vertex from the closed neighborhood of v.

The following multiplicative connectivity indices of a graph were introduced by Kulli in [3]. They are defined as follows:

*Corresponding author: Kulli V.R

Department of Mathematics, Gulbarga University, Gulbarga 585106, India

The multiplicative product connectivity index of a graph G is defined as

$$PII(G) = \tilde{O}_{uv\hat{1} E(G)} \frac{1}{\sqrt{d_G(u)d_G(v)}}.$$

The multiplicative sum connectivity index of a graph G is defined as

$$SII(G) = \tilde{O}_{uv\hat{1} E(G)} \frac{1}{\sqrt{d_G(u) + d_G(v)}}.$$

The multiplicative atom bond connectivity index of a graph G is defined as

$$ABCII(G) = \bigcap_{u \lor \hat{1}} \sqrt{\frac{d_G(u) + d_G(v) - 2}{d_G(u)d_G(v)}}.$$

The multiplicative geometric-arithmetic index of a graph G is defined as

$$GAII(G) = \tilde{O}_{uv\hat{I} E(G)} \frac{2\sqrt{d_G(u)d_G(v)}}{d_G(u) + d_G(v)}.$$

Motivated by the definitions of the multiplicative connectivity indices and their applications, we introduce the multiplicative product connectivity ve-degree index, multiplicative sum connectivity ve-degree index, multiplicative atom bond connectivity ve-degree index and multiplicative geometricarithmetic ve-degree index of a graph as follows:

The multiplicative product connectivity ve-degree index of a graph G is defined as

$$P_{ve}II(G) = \tilde{O}_{uv\hat{1} E(G)} \frac{1}{\sqrt{d_{ve}(u)d_{ve}(v)}}.$$

The multiplicative sum connectivity ve-degree index of a graph G is defined as

$$S_{ve}II(G) = \tilde{O}_{uv\hat{1} E(G)} \frac{1}{\sqrt{d_{ve}(u) + d_{ve}(v)}}$$

The multiplicative atom bond connectivity ve-degree index of a graph G is defined as

$$ABC_{ve}II(G) = \tilde{O}_{uv\hat{1} E(G)} \sqrt{\frac{d_{ve}(u) + d_{ve}(v) - 2}{d_{ve}(u)d_{ve}(v)}}.$$

The multiplicative geometric-arithmetic ve-degree index of a graph G is defined as

$$GA_{ve}II(G) = \bigcap_{uv\hat{1}} \frac{2\sqrt{d_{ve}(u)d_{ve}(v)}}{d_{ve}(u) + d_{ve}(v)}.$$

Recently, some ve-degree topological indices were studied, for example, in [4, 5, 6, 7, 8].

We consider the families of dominating oxide networks and regular triangulate oxide networks [9, 10]. In this paper, we compute the multiplicative connectivity ve-degree indices for dominating oxide networks (DOX) and regular triangulate oxide networks (RTOX).

Results For Dominating Oxide Networks DOX(n)

The molecular structure of a dominating oxide network is presented in Figure 1. The family of oxide networks is symbolized by DOX(n).

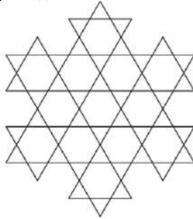


Figure 1 The structure of a dominating oxide network

In [9], Ediz obtained the partition of the edges with respect to their sum degree of end vertices of dominating oxide networks in Table 1.

Table 1

$(S_u, S_v) \setminus uv \in E(G)$	(8, 12)	(8, 14)	(12, 12)	(12, 14)	(14, 16)	(16, 16)
Number of edges	12n	12 <i>n</i> –12	6	12 <i>n</i> –12	24n-24	$54n^2 - 114n + 60$

Also he has given the ve-degree partition of the end vertices of edges for dominating oxide networks in Table 2.

Table 2

$$(d_{ve}(u), d_{ve}(v)) \setminus uv \in E(G)$$
 (7, 10) (7, 12) (10, 10) (10, 12) (12, 14) (14, 14)
Number of edges 12n 12n-12 6 12n-12 24n-24 54n²-114n+60

We now compute multiplicative connectivity ve-degree indices of DOX(n). (1)

Theorem 1: The multiplicative product connectivity ve-degree index of a dominating oxide network DOX(n) is

$$P_{ve} H \left(DOX(n)\right) = \underbrace{\frac{\alpha}{6}1}_{670\overline{\phi}} \underbrace{\frac{\delta^{6n}}{\frac{1}{2}}}_{684\overline{\phi}} \cdot \underbrace{\frac{\alpha}{6}1}_{684\overline{\phi}} \underbrace{\frac{\delta^{6n-6}}{\frac{1}{2}}}_{610\overline{\phi}} \cdot \underbrace{\frac{\alpha}{6}1}_{6120\overline{\phi}} \underbrace{\frac{\delta^{6n-6}}{\frac{1}{2}}}_{6120\overline{\phi}} \cdot \underbrace{\frac{\alpha}{6}1}_{6168\overline{\phi}} \underbrace{\frac{\delta^{2n-12}}{\frac{1}{2}}}_{6168\overline{\phi}} \cdot \underbrace{\frac{\alpha}{6}1}_{614\overline{\phi}} \underbrace{\frac{\delta^{4n^2-114n+60}}{\frac{1}{2}}}_{614\overline{\phi}}.$$

Proof: Let G be the molecular graph of a dominating oxide network DOX(n). By using equation (1) and Table 2, we deduce

$$\begin{split} &P_{ve} II \left(DOX\left(n\right)\right) = \underbrace{\tilde{O}}_{uv\hat{1}} \underbrace{\frac{1}{E(G)} \sqrt{d_{ve}\left(u\right)} d_{ve}\left(v\right)}_{u\hat{1}d_{ve}\left(v\right)} \\ &= \underbrace{\tilde{e}}_{v} \underbrace{\frac{1}{V}}_{v} \underbrace{\tilde{O}}_{v}^{\frac{1}{2}n} \cdot \underbrace{\tilde{e}}_{v} \underbrace{\frac{1}{V}}_{v} \underbrace{\tilde{O}}_{v}^{\frac{1}{2}n-12} \cdot \underbrace{\tilde{e}}_{v} \underbrace{\tilde{O}}_{v}^{\frac{1}{2}n-12} \cdot \underbrace{\tilde{O}}_{v}^{\frac{1}{2$$

Theorem 2: The multiplicative sum connectivity ve-degree index of a dominating oxide network DOX(n) is

Proof: Let G be the molecular graph of a dominating oxide network DOX(n). By using equation (2) and Table 2, we deduce

$$\begin{split} S_{ve} II \left(DOX\left(n\right)\right) &= \underbrace{\tilde{O}}_{uv\hat{1}} \underbrace{\frac{1}{E(G)} \sqrt{d_{ve}\left(u\right) + d_{ve}\left(v\right)}}_{v\hat{1}} \\ &= \underbrace{\frac{a}{k}}_{\sqrt{7+10}} \underbrace{\frac{\dot{\sigma}^{12n}}{\dot{\tau}}}_{\frac{1}{2}}, \underbrace{\frac{a}{k}}_{\sqrt{7+12}} \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{1}{2}}, \underbrace{\frac{a}{k}}_{\sqrt{10+10}} \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{1}{2}}, \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\sqrt{10+12}} \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{1}{2}}, \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{1}{2}} \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{1}{2}} \\ &= \underbrace{\frac{\dot{\sigma}^{1}}_{17}}_{\frac{17}{2}}, \underbrace{\frac{\dot{\sigma}^{1}}_{21}}_{\frac{17}{2}} \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{17}{2}}, \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{17}{2}}, \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{17}{2}}, \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{17}{2}} \underbrace{\frac{\dot{\sigma}^{12n-12}}{\dot{\tau}}}_{\frac{17}{2}}$$

Theorem 3: The multiplicative atom bond connectivity vedegree index of a dominating oxide network DOX(n) is

$$ABC_{ve}II(DOX(n)) = \underbrace{\overset{33}{610}}_{114\vec{p}}^{6n} \cdot \underbrace{\overset{47}{6}^{6n}}_{884\vec{p}}^{6n} \cdot \underbrace{\overset{29}{69}}_{150\vec{p}}^{3} \cdot \underbrace{\overset{41}{60}^{6n}}_{150\vec{p}}^{6n} \cdot \underbrace{\overset{41}{60}}_{17\vec{p}}^{6n-6} \cdot \underbrace{\overset{41}{60}}_{17\vec{p}}^{6n-12} \cdot \underbrace{\overset{41}{600}}_{17\vec{p}}^{327n^2-57n+30}.$$

Proof: Let G be the molecular graph of a dominating oxide network DOX(n). By using equation (3) and Table 2, we deduce

$$\begin{split} ABC_{ve} II \left(DOX\left(n\right)\right) &= \underbrace{\tilde{O}}_{uv\hat{1}}\underbrace{\frac{d_{ve}\left(u\right) + d_{ve}\left(v\right) - 2}}_{dve} \underbrace{\frac{d_{ve}\left(u\right) d_{ve}\left(v\right)}{d_{ve}\left(u\right) d_{ve}\left(v\right)}}_{dve} \\ &= \underbrace{\tilde{E}}_{v}^{\frac{7+10-2}{7'10}}\underbrace{\frac{\ddot{O}^{2n}}{\ddot{c}}}_{\frac{\dot{c}}{2}} \underbrace{\tilde{E}}_{v}^{\frac{7+12-2}{2}}\underbrace{\frac{\ddot{O}^{2n-12}}{\ddot{c}}}_{\frac{\dot{c}}{2}} \underbrace{\tilde{E}}_{v}^{\frac{10+10-2}{2}}\underbrace{\frac{\ddot{O}^{2n-12}}{10'10}}_{\frac{\dot{c}}{2}} \underbrace{\tilde{E}}_{v}^{\frac{10+12-2}{2}}\underbrace{\frac{\ddot{O}^{2n-12}}{10'12}}_{\frac{\dot{c}}{2}} \underbrace{\tilde{E}}_{v}^{\frac{10+12-2}{2}}\underbrace{\frac{\ddot{O}^{2n-12}}{\ddot{c}}}_{\frac{\dot{c}}{2}} \\ &= \underbrace{\tilde{E}}_{14}^{\frac{3}{2}}\underbrace{\tilde{O}^{6n-6}}_{\frac{\dot{c}}{2}} \underbrace{\tilde{E}}_{34}^{\frac{3}{2}} \underbrace{\tilde{E}}_{50}^{\frac{3}{2}} \underbrace{\tilde{E}}_{50}^{\frac{3}{2}} \underbrace{\tilde{E}}_{60}^{\frac{3}{2}} \underbrace{\tilde{E}}_{60}^{\frac{3}{2}} \underbrace{\tilde{E}}_{50}^{\frac{3}{2}} \underbrace{\tilde{E}}_{50}^{\frac{3}{2}} \underbrace{\tilde{E}}_{60}^{\frac{3}{2}} \underbrace{\tilde{E}}_{60}^{\frac$$

Theorem 4: The multiplicative geometric-arithmetic ve-degree index of a dominating oxide network DOX(n) is

$$GA_{ve}II\left(DOX\left(n\right)\right) = \underbrace{\frac{22\sqrt{70}}{5}}_{k}^{2}\frac{\sqrt{70}}{17}\underbrace{\frac{\ddot{0}^{12n}}{\ddot{0}}}^{\frac{12n}{3}} \cdot \underbrace{\frac{24\sqrt{21}}{5}}_{k}^{\frac{32n-12}{3}} \cdot \underbrace{\frac{22\sqrt{30}}{5}}_{k}^{\frac{32n-12}{3}} \cdot \underbrace{\frac{22\sqrt{30}}{5}}_{k}^{\frac{32n-12}{3}} \cdot \underbrace{\frac{22\sqrt{42}}{5}}_{k}^{\frac{324n-24}{3}}.$$

Proof: Let G be the molecular graph of a dominating oxide network DOX(n). By using equation (4) and Table 2, we deduce

$$\begin{split} GA_{ve} II \big(DOX\,(n)\big) &= \underbrace{\tilde{O}}_{uv\hat{1}\,E(G)} \frac{2\sqrt{d_{ve}(u)d_{ve}(v)}}{d_{ve}(u) + d_{ve}(v)} \\ &= \underbrace{\tilde{C}}_{ve}^{2\sqrt{7'}} \frac{10}{0} \underbrace{\tilde{O}}_{ve}^{12n} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{7'}} \frac{12}{0} \underbrace{\tilde{O}}_{ve}^{12n-12} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{10'}} \frac{10}{0} \underbrace{\tilde{O}}_{ve}^{6} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{10'}} \frac{12}{0} \underbrace{\tilde{O}}_{ve}^{12n-12} \\ &= \underbrace{\tilde{C}}_{ve}^{2\sqrt{7'}} \frac{10}{0} \underbrace{\tilde{O}}_{ve}^{12n-24} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{10'}} \frac{10}{0} \underbrace{\tilde{O}}_{ve}^{12n-12} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{10'}} \frac{10}{0} \underbrace{\tilde{O}}_{ve}^{12n-12} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{10'}} \frac{12}{0} \underbrace{\tilde{O}}_{ve}^{2\sqrt{10'}} \underbrace{\tilde{O}}_{ve}^{12n-12} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{10'}} \frac{12}{0} \underbrace{\tilde{O}}_{ve}^{12n-12} \cdot \underbrace{\tilde{C}}_{ve}^{2\sqrt{10'}} \frac{12}{0} \underbrace{\tilde{O}}_{ve}^{2\sqrt{10'}} \underbrace$$

Results For Regular Triangulate Oxide Networks RTOX(n)

The molecular structure of a regular triangulate oxide network is presented in Figure 2. The family of regular triangulate oxide networks is denoted by RTOX(n), $n \ge 3$.

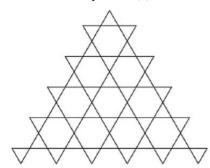


Figure 2 The graph of a regular triangulate oxide network RTOX(5)

In [9], Ediz has given the partition of the edges with respect to their sum degree of end vertices of regular triangulate oxide networks in Table 3.

Table 3

(S_u, S_v)	(6,6)	(6,12)	(8,12)	(8,14)	(12,12)	(12,14)	(14,14)	(14,16)	(16, 16)
Number of	2	4	4	6n-8	1	6	6n-9	6n-12	$3n^{2}$
edges	2	4	4	on-o	1	U	0 <i>n</i> -9	011-12	12n+12

Also he has given the ve-degree partition of the end vertices of edges for regular triangulate oxide networks in Table 4.

Table 4

$(d_{ve}(u), d_{ve}(v))$	(5,5)	(5,10)	(7,10)	(7,12)	(10,10)	(10,12)	(12,12)	(12,14)	(14,14)
Number of edges	2	4	4	6n-8	1	6	6n-9	6n-12	$3n^2$ - $12n+12$

We now compute the multiplicative product connectivity vedegree index of RTOX(n).

Theorem 5: The multiplicative product connectivity ve-degree index of a regular triangulate oxide network RTOX(n) is

$$\begin{split} P_{ve}II(RTOX(n)) &= \underbrace{\frac{\alpha_{0}^{1}}{5^{\frac{3}{2}}}}_{55\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{55\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{570\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{510\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{510\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{5120\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{584\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{584\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{512\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{5120\overline{\phi}} \underbrace{\frac{\alpha_{1}^{1}}{5^{\frac{3}{2}}}}_{5$$

Proof: Let G be the molecular graph of a regular triangulate oxide network RTOX(n). By using equation (1) and Table 4, we deduce

$$\begin{split} &P_{ve}II(RTOX(n)) = \underbrace{\tilde{O}}_{uv\hat{1}} \underbrace{\frac{1}{E(G)}\sqrt{d_{ve}(u)d_{ve}(v)}}_{lv\hat{1}} \\ &= \underbrace{\frac{a}{k}}_{u\hat{1}} \underbrace{\frac{\ddot{O}^{2}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{u\hat{5}^{2}} \underbrace{\frac{\ddot{O}^{4}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{u\hat{5}^{2}} \underbrace{\frac{\ddot{O}^{4}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{u\hat{5}^{2}} \underbrace{\frac{\ddot{O}^{6n-9}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{u\hat{5}^{2}} \underbrace{\frac{\ddot{O}^{6n-9}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{u\hat{5}^{2}} \underbrace{\frac{\ddot{O}^{6n-12}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{u\hat{5}^{2}} \underbrace{\frac{\ddot{O}^{6n-12}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{u\hat{5}^{2}} \underbrace{\frac{\ddot{O}^{3n^{2}-12n+12}}{\ddot{0}^{2}}}_{u\hat{5}^{2}} \\ &= \underbrace{\frac{a}{k}}_{0} \underbrace{\ddot{O}^{2}}_{0} \underbrace{\frac{a}{k}}_{0} \underbrace{\ddot{O}^{2}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{0} \underbrace{\ddot{O}^{2}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{0} \underbrace{\ddot{O}^{3n^{2}-12n+12}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{0} \underbrace{\ddot{O}^{3n^{2}-12n+12}}_{u\hat{5}^{2}} \\ &= \underbrace{\frac{a}{k}}_{0} \underbrace{\ddot{O}^{2}}_{0} \underbrace{\frac{a}{k}}_{0} \underbrace{\ddot{O}^{3n^{2}-12n+12}}_{u\hat{5}^{2}} \underbrace{\frac{a}{k}}_{0} \underbrace{\overset{O}^{3n^{2$$

Theorem 6. The multiplicative sum connectivity ve-degree index of a regular triangulate oxide network RTOX(n) is

$$S_{ve}II(RTOX(n)) = \underbrace{\frac{\alpha 1}{6} \frac{\ddot{0}}{10 \dot{\phi}}}_{\text{ξ10}} \cdot \underbrace{\frac{\alpha 1}{6} \frac{\ddot{0}^{2}}{15 \dot{\phi}}}_{\text{ξ10}} \cdot \underbrace{\frac{\alpha 1}{6} \frac{\ddot{0}^{2}}{17 \dot{\phi}}}_{\text{ξ10}} \cdot \underbrace{\frac{\alpha 1}{6} \frac{\ddot{0}^{2}}{120 \dot{\phi}}}_{\text{ξ10}} \cdot \underbrace{\frac{\alpha 1}{6} \frac{\ddot{0}^{3n-4}}{120 \dot{\phi}}}_{\text{ξ10}} \cdot \underbrace{\frac$$

Proof: Let G be the molecular graph of a regular triangulate oxide network TROX(n). By using equation (2) and Table 4, we deduce

$$S_{ve}II(TROX(n)) = \underbrace{\tilde{O}}_{uv\hat{1}} \underbrace{\frac{1}{E(G)}\sqrt{d_{ve}(u) + d_{ve}(v)}}_{uv\hat{1}}$$

$$= \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{\sqrt{5+5}}}_{\frac{1}{\xi}}^{\frac{2}{\xi}}}_{\sqrt{5+5}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\frac{1}{\xi}}^{\frac{4}{\xi}}}_{\sqrt{5+10}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\frac{1}{\xi}}^{\frac{4}{\xi}}}_{\sqrt{7+10}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\frac{1}{\xi}}^{\frac{4}{\xi}}}_{\sqrt{7+12}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\frac{1}{\xi}}^{\frac{4}{\xi}}}_{\sqrt{10+10}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{10+10}}^{\frac{4}{\xi}}}_{\sqrt{10+10}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{12+14}}^{\frac{4}{\xi}}}_{\sqrt{12+14}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}$$

$$= \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{10}^{\frac{4}{\xi}}}_{\sqrt{10+12}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{17}^{\frac{4}{\xi}}}_{\sqrt{12+14}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{12+14}}^{\frac{4}{\xi}}}_{\sqrt{12+14}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}$$

$$= \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{10}^{\frac{4}{\xi}}}_{\sqrt{15+10}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{15+10}}^{\frac{4}{\xi}}}_{\sqrt{12+14}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{20}} \underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}$$

$$\underbrace{\underbrace{\frac{a}{\xi} \underbrace{\frac{1}{0}}_{\sqrt{12+12}}^{\frac{4}{\xi}}}_{\sqrt{12+14}}^{\frac{4}{\xi}}}_{\sqrt{12+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}}_{\sqrt{14+14}}^{\frac{4}{\xi}}$$

Theorem 7: The multiplicative atom bond connectivity vedegree index of a regular triangulate oxide network RTOX(n) is

$$ABC_{ve}II(RTOX(n)) = \underbrace{\frac{88}{625}}_{\frac{1}{2}}^{\frac{1}{2}} \cdot \underbrace{\frac{813}{6}}_{500}^{\frac{1}{2}} \cdot \underbrace{\frac{81}{6}}_{140}^{\frac{1}{2}} \cdot \underbrace{\frac{87}{2}}_{6840}^{\frac{1}{2}}^{\frac{1}{2}} \cdot \underbrace{\frac{83}{2}}_{1000}^{\frac{1}{2}} \cdot \underbrace{\frac{81}{6}}_{\frac{1}{2}}^{\frac{1}{2}} \cdot \underbrace{\frac{11}{6}}_{\frac{1}{2}}^{\frac{1}{2}} \cdot \underbrace{\frac{11}{6}}_{\frac{1}$$

Proof: Let G be the molecular graph of a dominating oxide network RTOX(n). By using equation (3) and Table 4, we deduce

$$ABC_{ve}II\left(RTOX\left(n\right)\right) = \bigcap_{u \neq 1} \sqrt{\frac{d_{ve}\left(u\right) + d_{ve}\left(v\right) - 2}{d_{ve}\left(u\right)d_{ve}\left(v\right)}}$$

$$= \underbrace{\frac{x}{6}} \sqrt{\frac{5+5-2}{5'}} \underbrace{\frac{0^2}{\frac{1}{2}}}, \underbrace{\frac{x}{6}} \sqrt{\frac{5+10-2\frac{0^4}{\frac{1}{2}}}{5'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{7+10-2\frac{0^4}{\frac{1}{2}}}{7'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{7+12-2\frac{0^6}{\frac{1}{2}}}{7'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{7'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{7'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{7'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{10'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{10'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{10'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10+10-2\frac{0^4}{\frac{1}{2}}}{12'}}, \underbrace{\frac{x}{6}} \sqrt{\frac{10-10-2\frac{0^4}{\frac{10-10-2}{\frac$$

Theorem 8: The multiplicative geometric-arithmetic ve-degree index of a regular triangulate oxide network RTOX(n) is

$$GA_{ve}H\left(RTOX\left(n\right)\right) = \underbrace{\frac{32\sqrt{2}}{5}\frac{2^d}{3}}_{\frac{7}{6}} \cdot \underbrace{\frac{32\sqrt{70}}{5}\frac{2^d}{5}}_{\frac{7}{6}} \cdot \underbrace{\frac{24\sqrt{21}}{5}\frac{2^{6n-8}}{6}}_{\frac{7}{6}} \cdot \underbrace{\frac{32\sqrt{30}}{5}\frac{2^6}{5}}_{\frac{7}{6}} \cdot \underbrace{\frac{32\sqrt{42}}{5}\frac{2^{6n-12}}{6}}_{\frac{7}{6}} \cdot \underbrace{\frac{32\sqrt{42}}{5}\frac{2^{6n-12}}{5}}_{\frac{7}{6}} \cdot \underbrace{\frac{32\sqrt{42}}{5}\frac{2^{6n-12}}{5}}_{\frac{7}{6}}$$

Proof: Let G be the molecular graph of a regular triangulate oxide network RTOX(n). By using equation (4) and Table 4, we deduce

$$ABC_{ve}II\left(RTOX\left(n\right)\right) = \underbrace{\tilde{O}}_{uv\hat{1}} \underbrace{\frac{2\sqrt{d_{ve}\left(u\right)d_{ve}\left(v\right)}}{d_{ve}\left(u\right) + d_{ve}\left(v\right)}}_{uv\hat{1}}$$

$$= \underbrace{\frac{32\sqrt{5' \cdot 5}\frac{\vec{O}}{2}}{5 + 5 \cdot \frac{\vec{O}}{2}}}_{5 + 5 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{5' \cdot 10}\frac{\vec{O}}{2}}{5 + 10 \cdot \frac{\vec{O}}{2}}}_{5 + 10 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{7' \cdot 10}\frac{\vec{O}}{2}}{7 + 10 \cdot \frac{\vec{O}}{2}}}_{7 + 10 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{7' \cdot 12}\frac{\vec{O}}{2}}{7 + 12 \cdot \frac{\vec{O}}{2}}}_{10 + 10 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{10' \cdot 12}\frac{\vec{O}}{2}}{10 + 12 \cdot \frac{\vec{O}}{2}}}_{10 + 12 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{12' \cdot 12}\frac{\vec{O}}{2}}{12 + 12 \cdot \frac{\vec{O}}{2}}}_{12 + 12 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{12' \cdot 14}\frac{\vec{O}}{2}}{12 + 14 \cdot \frac{\vec{O}}{2}}}_{12 + 14 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{14' \cdot 14}\frac{\vec{O}}{2}}{14 + 14 \cdot \frac{\vec{O}}{2}}}_{12 + 14 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{14' \cdot 14}\frac{\vec{O}}{2}}{14 + 14 \cdot \frac{\vec{O}}{2}}}_{12 + 12 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{12' \cdot 12}\frac{\vec{O}}{2}}_{12 + 12 \cdot \frac{\vec{O}}{2}}}_{12 + 12 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{12' \cdot 12}\frac{\vec{O}}{2}}_{12 + 12 \cdot \frac{\vec{O}}{2}}}_{13 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{32\sqrt{12' \cdot 12}\frac{\vec{O}}{2}}_{13 \cdot \frac{\vec{O}}{2}}}_{13 \cdot \frac{\vec{O}}{2}} \underbrace{\frac{\vec{O}}{2}}_{13 \cdot \frac{\vec{O}}{2}}$$

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How to cite this article:

Kulli V.R (2018) 'Multiplicative Connectivity Ve-Degree indices of Dominating Oxide And Regular Triangulate Oxide Networks', *International Journal of Current Advanced Research*, 07(4), pp. 11961-11964. DOI: http://dx.doi.org/10.24327/ijcar.2018.11964.2089
