

DEGREE BASED MULTIPLICATIVE CONNECTIVITY INDICES OF NANOSTRUCTURES

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ABSTRACT

In Chemical Graph Theory, connectivity indices have been found useful in practical application. In this paper, we compute the multiplicative product connectivity index, multiplicative sum connectivity index and geometric-arithmetic index of certain nanotubes and nanotorus.

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INTRODUCTION

All graphs considered here are finite, simple connected graphs. Let G be a connected graph with vertex set $V(G)$ and edge set $E(G)$. The degree $d_G(v)$ of a vertex v is the number of vertices adjacent to v . For all further notation and terminology, we refer to the reader to [1].

A molecular graph is a finite simple graph such that its vertices correspond to the atoms and the edges to the bonds. Chemical graph theory is a branch of Mathematical Chemistry which has an important effect on the development of Chemical Sciences. There are many connectivity indices that have some applications in Chemistry, see [2].

Motivated by the definition of the product connectivity index and its wide applications, Kulli [3] introduced the multiplicative product connectivity index, multiplicative sum connectivity index and multiplicative geometric-arithmetic index of a molecular graph as follows:

The multiplicative product connectivity index of a graph G is defined as

$$PII(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{d_G(u)d_G(v)}}$$

The multiplicative sum connectivity index of a graph G is defined as

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$$SII(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{d_G(u) + d_G(v)}}$$

The multiplicative geometric-arithmetic index of a graph G is defined as

$$GAI(G) = \prod_{uv \in E(G)} \frac{2\sqrt{d_G(u)d_G(v)}}{d_G(u) + d_G(v)}$$

Recently, several multiplicative indices were studied, for example, in [4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18]. Also some connectivity indices were studied, for example, in [19, 20, 21, 22, 23, 24, 25, 26]. In this paper, we compute the multiplicative product connectivity index, multiplicative sum connectivity index and multiplicative geometric-arithmetic index of $TUC_4C_8(S)$ nanotubes and $TUC_4C_8(R)$ nanotorus. For more information about nanotubes and nanotorus see [27].

$KTUC_4C_8(S)$ Nanotubes

In this section, we consider a family of $TUC_4C_8(S)$ nanotubes.

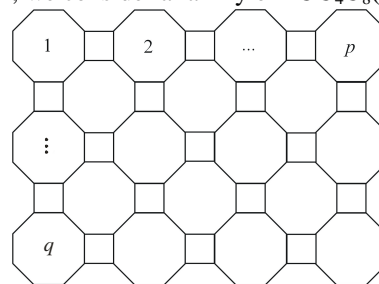


Figure 1 The graph of $KTUC_4C_8[p,q]$ nanotube

The 2-dimensional lattice of $TUC_4C_8(S)$ is denoted by $K=KTUC_4C_8[p,q]$ where q is the number of rows and p is the number of columns, see Figure 1.

Let K be the molecular graph of $KTUC_4C_8[p,q]$ nanotube. By calculation, we obtain that K has three types of edges based on the degree of end vertices of each edge as given in Table 1.

Table 1 Edge partition of K

$d_K(u), d_K(v) uv \in E(K)$	(2, 2)	(2, 3)	(3, 3)
Number of edges	$2p+2q+4$	$4p+4q-8$	$12pq - 8(p+q)+4$

Theorem 1: The multiplicative product connectivity index of $KTUC_4C_8[p,q]$ nanotube is

$$PII(KTUC_4C_8[p,q]) = \left(\frac{1}{2}\right)^{2p+2q+4} \times \left(\frac{1}{6}\right)^{2p+2q-4} \times \left(\frac{1}{3}\right)^{12pq-8(p+q)+4}$$

Proof: By definition, we have

$$PII(K) = \prod_{uv \in E(K)} \frac{1}{\sqrt{d_K(u)d_K(v)}}$$

By using Table 1, we deduce

$$PII(KTUC_4C_8[p,q]) = \left(\frac{1}{\sqrt{2 \times 2}}\right)^{2p+2q+4} \times \left(\frac{1}{\sqrt{2 \times 3}}\right)^{4p+4q-8} \times \left(\frac{1}{\sqrt{3 \times 3}}\right)^{12pq-8(p+q)+4}$$

$$= \left(\frac{1}{2}\right)^{2p+2q+4} \times \left(\frac{1}{6}\right)^{2p+2q-4} \times \left(\frac{1}{3}\right)^{12pq-8(p+q)+4}$$

Theorem 2: The multiplicative sum connectivity index of $KTUC_4C_8[p,q]$ nanotube is

$$SII(KTUC_4C_8[p,q]) = \left(\frac{1}{2}\right)^{2p+2q+4} \times \left(\frac{1}{5}\right)^{2p+2q-4} \times \left(\frac{1}{6}\right)^{6pq-4(p+q)+2}$$

Proof: By definition, we have

$$SII(K) = \prod_{uv \in E(K)} \frac{1}{\sqrt{d_K(u) + d_K(v)}}$$

By using Table 1, we have

$$SII(KTUC_4C_8[p,q]) = \left(\frac{1}{\sqrt{2+2}}\right)^{2p+2q+4} \times \left(\frac{1}{\sqrt{2+3}}\right)^{4p+4q-8} \times \left(\frac{1}{\sqrt{3+3}}\right)^{12pq-8(p+q)+4}$$

$$= \left(\frac{1}{2}\right)^{2p+2q+4} \times \left(\frac{1}{5}\right)^{2p+2q-4} \times \left(\frac{1}{6}\right)^{6pq-4(p+q)+2}$$

Theorem 3: The multiplicative geometric-arithmetic index of $KTUC_4C_8[p,q]$ nanotube is

$$GAI(KTUC_4C_8[p,q]) = \left(\frac{2\sqrt{6}}{5}\right)^{4p+4q-8}$$

Proof: By definition, we have

$$GAI(K) = \prod_{uv \in E(K)} \frac{2\sqrt{d_K(u)d_K(v)}}{d_K(u) + d_K(v)}$$

By using Table 1, we deduce

$$GAI(KTUC_4C_8[p,q]) = \left(\frac{2\sqrt{2 \times 2}}{2+2}\right)^{2p+2q+4} \times \left(\frac{2\sqrt{2 \times 3}}{2+3}\right)^{4p+4q-8} \times \left(\frac{2\sqrt{3 \times 3}}{3+3}\right)^{12pq-8(p+q)+4}$$

$$= \left(\frac{2\sqrt{6}}{5}\right)^{4p+4q-8}$$

$GTUC_4C_8(S)$ Nanotubes

In this section, we consider a family of $TUC_4C_8(S)$ nanotubes. The 2-dimensional lattice of $TUC_4C_8(S)$ is denoted by

$G=GTUC_4C_8[p,q]$ where q is the number of rows and p is the number of columns, see Figure 2.

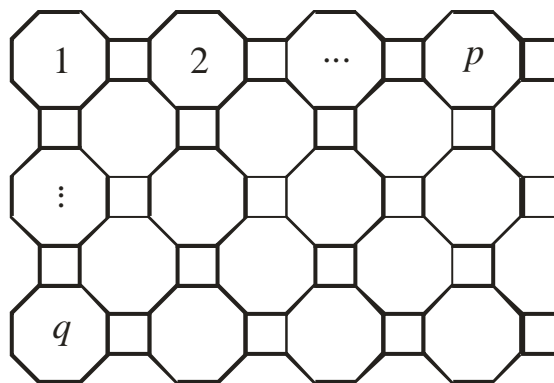


Figure 2 The graph of $GTUC_4C_8[p,q]$ nanotube

Let G be the molecular graph of $GTUC_4C_8[p,q]$ nanotube. By calculation, we obtain that G has three types of edges based on the degree of end vertices of each edge as given in Table 2.

Table 2 Edge partition of G

$d_G(u), d_G(v) uv \in E(G)$	(2, 2)	(2, 3)	(3, 3)
Number of edges	$2p$	$4p$	$12pq - 8p$

Theorem 4: The multiplicative product connectivity index of $GTUC_4C_8[p,q]$ nanotube is

$$PII(GTUC_4C_8[p,q]) = \left(\frac{1}{2}\right)^{2p} \times \left(\frac{1}{6}\right)^{2p} \times \left(\frac{1}{3}\right)^{12pq-8p}$$

Proof: By definition, we have

$$PII(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{d_G(u)d_G(v)}}$$

By using Table 1, we derive

$$PII(GTUC_4C_8[p,q]) = \left(\frac{1}{\sqrt{2 \times 2}}\right)^{2p} \times \left(\frac{1}{\sqrt{2 \times 3}}\right)^{4p} \times \left(\frac{1}{\sqrt{3 \times 3}}\right)^{12pq-8p}$$

$$= \left(\frac{1}{2}\right)^{2p} \times \left(\frac{1}{6}\right)^{2p} \times \left(\frac{1}{3}\right)^{12pq-8p}$$

Theorem 5: The multiplicative sum connectivity index of $GTUC_4C_8[p,q]$ nanotube is

$$SII(GTUC_4C_8[p,q]) = \left(\frac{1}{2}\right)^{2p} \times \left(\frac{1}{5}\right)^{2p} \times \left(\frac{1}{6}\right)^{6pq-4p}$$

Proof: By definition, we derive

$$SII(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{d_G(u) + d_G(v)}}$$

By using Table 1, we have

$$SII(GTUC_4C_8[p,q]) = \left(\frac{1}{\sqrt{2+2}}\right)^{2p} \times \left(\frac{1}{\sqrt{2+3}}\right)^{4p} \times \left(\frac{1}{\sqrt{3+3}}\right)^{12pq-8p}$$

$$= \left(\frac{1}{2}\right)^{2p} \times \left(\frac{1}{5}\right)^{2p} \times \left(\frac{1}{6}\right)^{6pq-4p}$$

Theorem 6: The multiplicative geometric-arithmetic index of $GTUC_4C_8[p,q]$ nanotube is

$$GAI(GTUC_4C_8[p,q]) = \left(\frac{2\sqrt{6}}{5}\right)^{4p}$$

Proof: By definition, we have

$$GAI(G) = \prod_{uv \in E(G)} \frac{2\sqrt{d_G(u)d_G(v)}}{d_G(u) + d_G(v)}$$

By using Table 2, we deduce

$$GAI(GTUC_4C_8[p,q]) = \left(\frac{2\sqrt{2 \times 2}}{2+2}\right)^{2p} \times \left(\frac{2\sqrt{2 \times 3}}{2+3}\right)^{4p} \times \left(\frac{2\sqrt{3 \times 3}}{3+3}\right)^{12pq-8p}$$

$$= \left(\frac{2\sqrt{6}}{5}\right)^{4p}$$

HTUC₄C₈(R) Nanotorus

In this section, we consider a family of TUC₄C₈(R) nanotorus. The 2-dimensional lattice of TUC₄C₈(R) is denoted by H=HTUC₄C₈[p,q] where p is the number of columns and q is the number of rows, see Figure 3.

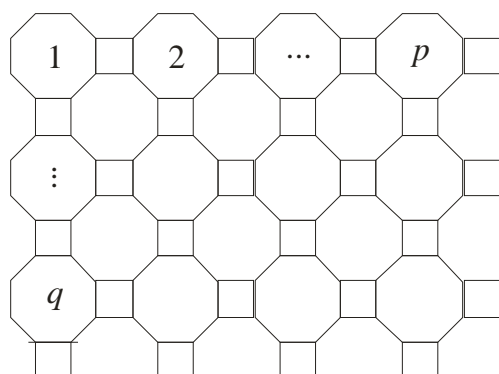


Figure 3 The graph of HTUC₄C₈[p,q] nanotorus

Let H be the graph of HTUC₄C₈[p,q] nanotorus. By calculation, we obtain that H has one type of edges based on the degree of end vertices of each edge as given in Table 3.

Table 3 Edge partition of H

$d_H(u), d_H(v) \setminus uv \in E(H)$	(3, 3)
Number of edges	12pq

Theorem 7. Let H be the graph of HTUC₄C₈[p,q] nanotorus. Then

1) $PII(HTUC_4C_8[p,q]) = \left(\frac{1}{3}\right)^{12pq}$

2) $SII(HTUC_4C_8[p,q]) = \left(\frac{1}{6}\right)^{6pq}$

3) $GAI(HTUC_4C_8[p,q]) = 1$

Proof: Let H be the graph of HTUC₄C₈[p,q] nanotorus. Now using Table 3, we deduce

1) $PII(HTUC_4C_8[p,q]) = \prod_{uv \in E(H)} \frac{1}{\sqrt{d_H(u)d_H(v)}}$

$$= \left(\frac{1}{\sqrt{3 \times 3}}\right)^{12pq} = \left(\frac{1}{3}\right)^{12pq}$$

2) $SII(HTUC_4C_8[p,q]) = \prod_{uv \in E(H)} \frac{1}{\sqrt{d_H(u) + d_H(v)}}$

$$= \left(\frac{1}{\sqrt{3+3}}\right)^{12pq} = \left(\frac{1}{6}\right)^{6pq}$$

3) $GAI(HTUC_4C_8[p,q]) = \prod_{uv \in E(H)} \frac{2\sqrt{d_H(u)d_H(v)}}{d_H(u) + d_H(v)}$

$$= \left(\frac{2\sqrt{3 \times 3}}{3+3}\right)^{12pq} = 1$$

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